

CA with FactoMineR and factoextra

Basics

CA (Correspondence Analysis) is a descriptive technique, that explains dependency between two categorical variable. It is usually applied to contingency tables — decomposes the chi-squared statistic into orthogonal factors, but may be applied to any table with nonnegative values.

It is conceptually similar to principal component analysis. The preprocessed contingency table is decomposed (Generalized Singular Value Decomposition) into a orthogonal profiles of rows and columns.

The Game of Thrones

This example uses the Kaggle dataset about battles in *Game of Thrones* (see <http://bit.ly/2qjUfQ2>). The **battles** table presents number of battles in which given House (row) was an attacking army with a given attacking strategy (column).

```
head(battles)
```

House	Battle_Type			
	ambush	pitched battle	razing	siege
Baratheon	0	2	0	3
Frey	1	0	0	2
Lannister	1	6	0	2
Stark	5	3	0	0
Tully	3	0	0	0

Use the **FactoMineR::CA()** function for correspondence analysis.

```
library("FactoMineR")
res.ca <- CA(battles, graph = FALSE)
summary(res.ca)
```

The chi square of independence between the two variables is equal to 25.82556 (p-value = 0.103814).

Eigenvalues

	Dim.1	Dim.2	Dim.3
Variance	0.362	0.201	0.099
% of var.	54.617	30.360	15.024
Cumulative % of var.	54.617	84.976	100.000

Rows

	Iner*1000	Dim.1	ctr	cos2
Baratheon	113.333	0.861	26.281	0.839
Bolton	45.299	-0.508	5.481	0.438
Frey	78.632	0.227	1.099	0.051
Greyjoy	83.333	-0.074	0.307	0.013
...				

Columns

	Iner*1000	Dim.1	ctr	cos2
ambush	217.236	-0.747	59.386	0.989
pitched battle	160.897	0.427	16.766	0.377
razing	99.359	-0.122	0.106	0.004
siege	184.701	0.579	23.742	0.465
...				

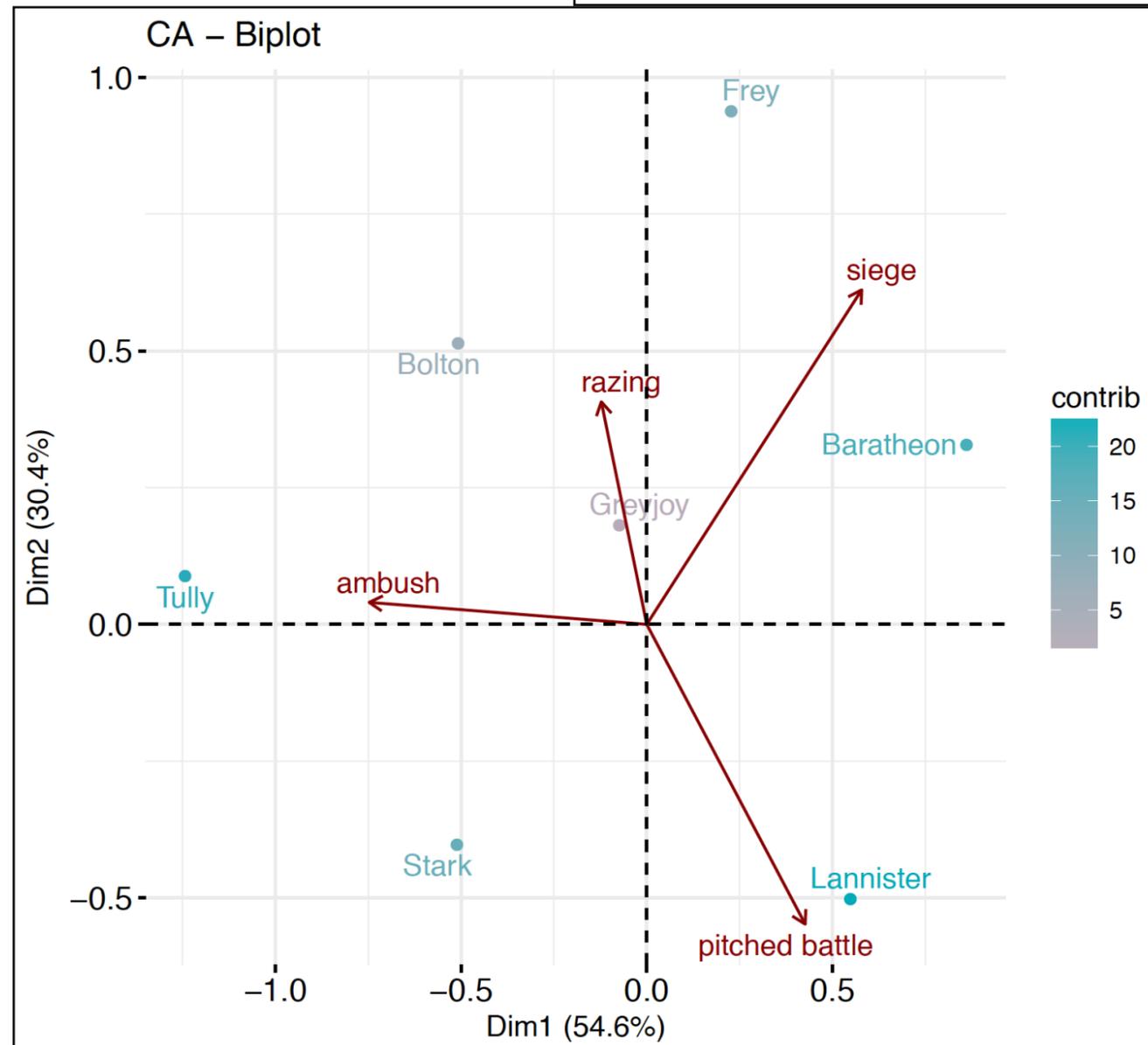
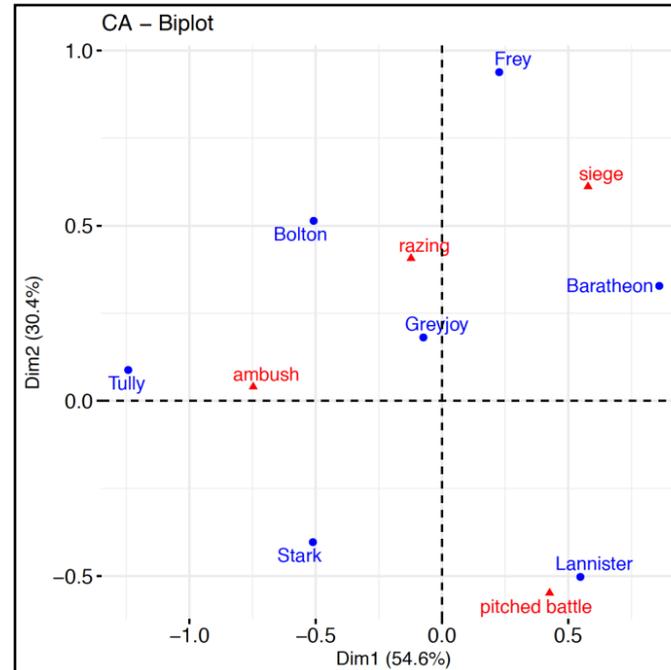
FactoMineR (for multivariate data analysis) and factoextra (for visualisation of CA results)

Biplots

Use the **factoextra::fviz_ca_biplot()** function to plot the biplot for a given model. Use **fviz_ca_row()** or **fviz_ca_col()** if you are interested only in profiles of rows/columns.

Consult the help page for numerous parameters of the **fviz_ca_biplot()** function, that allows to customise of biplot plots.

```
# Basic biplot, results in the right plot ->
fviz_ca_biplot(res.ca)
# Customised biplot, results in the bottom plot
fviz_ca_biplot(res.ca, repel = TRUE,
  arrow = c(FALSE, TRUE),
  col.row = "contrib",
  col.col = "red4",
  gradient.cols = c("#BBAFBB", "#00AFBB"))
```



Row/Column contributions plot

Use the **factoextra::fviz_contrib()** function to plot contributions of selected dimension (rows or columns) onto a selected axis.

Numerical values for contributions may be extracted with **get_ca_row()** or **get_ca_col()** functions.

```
# Row contributions to Dimension 1
fviz_contrib(res.ca, choice = "row", axes = 1)
# Column contributions to Dimension 1
fviz_contrib(res.ca, choice = "col", axes = 1)
# Numeric summaries
get_ca_col(res.ca)
Correspondence Analysis - Results for columns
=====
Name      Description
1 "$coord" "Coordinates for the columns"
2 "$cos2"  "Cos2 for the columns"
3 "$contrib" "contributions of the columns"
4 "$inertia" "Inertia of the columns"
```

